# The sensitivity of solsticial pauses to atmospheric ice and dust in the MarsWRF General Circulation Model

Christopher Lee<sup>a,b</sup>, Mark I. Richardson<sup>b</sup>, Claire. E. Newman<sup>b</sup>, Michael A. Mischna<sup>c</sup>

<sup>a</sup> University of Toronto, Toronto, Canada <sup>b</sup> Aeolis Research, Pasadena, California <sup>c</sup> Jet Propulsion Laboratory, California Institute of Technology, Pasadena, California

# Abstract

Mars exhibits less atmospheric variability at the solutions than it does during periods nearer the equinoxes. Much of this variability in air temperature and dust activity is attributable to a significant decrease in eastward traveling transient wave amplitudes in the lower atmosphere near the solstice. Previous versions of the Mars Weather Research and Forecasting (MarsWRF) model using only dust radiative forcing have reproduced the nature but not the magnitude of this 'solsticial pause' in atmospheric variability. In this paper, we use a version of MarsWRF that includes a fully-interactive dust and water cycle to simulate winter solsticial pauses under a range of dust and water ice conditions. The upgraded model specifically includes a new hybrid binned/two-moment microphysics model that simulates dust, water ice, and cloud condensation nuclei. The scheme tracks mass and number density for the three particle types throughout the atmosphere and allows advection by resolved winds, mixing by unresolved processes, and sedimentation that depends on particle size and density. Ice and dust particles interact with radiation in the atmosphere using a Mie scattering parameterization that

Preprint submitted to Icarus

December 6, 2017

allows for variable particle size and composition. Heterogeneous nucleation and condensation use an adaptive bin size scheme to accurately track the particle size during condensation and sublimation processes. All microphysical processes in the model are calculated within the dynamical timesteps using stability-guaranteed implicit calculations with no sub-timestepping. The impact of the addition of water processes to the model was assessed by comparing simulations with only interactive dust (dry simulations) and ones with a fully-interactive dust and water cycle (wet simulations). In dry simulations with dust storms a solsticial pause occurs in the northern winter with a magnitude (or 'depth') that depends on the opacity of the southern summer dust storms. In wet simulations that include water ice and dust particles, deep solsticial pauses are found in both winter hemispheres. In all simulations that reproduce the solution pause, energy and instability analysis suggest that a decrease in baroclinic instability and increase in barotropic energy conversion occurs during the solsticial pause. In dry simulations the decrease in baroclinic instability is caused by increased dust opacity leading to increased thermal static stability. In wet simulations, additional opacity from local cap-edge ice clouds reduces the near surface wind shear and further inhibits baroclinic eddy growth. The wet simulations are in better agreement with observations and tend to support results from other models that include ice cloud radiative effects.

Keywords: Mars, solsticial pause, transient waves, dust storms, ice clouds

### 1 1. Introduction

The Martian autumn and winter atmosphere is characterized by a relatively high degree of variability in the periods after the autumnal equinox 3 and before the vernal equinox, but with a distinct transition to much lower 4 variability centered on the winter solstice. This transition in the behavior of 5 the polar atmosphere is associated with a dramatic decrease in the number 6 of high latitude dust storms at solstice, as observed by the Mars Global Sur-7 vevor (MGS) Mars Orbiter Camera (MOC) (Wang et al., 2003, 2005, Wang, 8 2007, Guzewich et al., 2015), and a shift to both lower transient wave am-9 plitudes and longer wavelengths, as observed by the MGS Thermal Emission 10 Spectrometer (TES) (Banfield et al., 2004, Wang et al., 2005). 11

TES observations from just under three Martian years (1999-2006, MY24-12 27) are available within a gridded 'reanalysis' dataset (the Mars Analysis 13 Correction Data Assimilation (MACDA) reanalysis (Montabone et al., 2014)) 14 that highlights the 'solsticial pause' in particular detail (Lewis et al., 2016, 15 Wang and Toigo, 2016). The reanalysis dataset is especially useful as it pro-16 vides a uniform estimate of the global state of the atmosphere that is con-17 sistent with the more limited observations. As such, it can provide a clearer 18 basis for analysis and yield more robust diagnostics. Using the reanalysis, 19 Lewis et al. (2016) found a solsticial pause in both winter hemispheres with 20 a stronger solsticial pause during northern winter where temperature vari-21 ability drops by 50% in the near surface atmosphere, and a pause during 22 southern winter with a similar fractional depth but with smaller absolute 23 values. Wang and Toigo (2016) used the same reanalysis dataset to map the 24 relative stengths of the zonal wavenumber 1 to 3 eastward traveling waves 25

as a function of time during the transition into the pause in the northernhemisphere.

General Circulation Models (GCMs) have been used extensively to study 28 transient waves in the northern autumn and winter atmosphere (Barnes et al., 29 1993, Collins et al., 1996, Wilson et al., 2002, Kuroda et al., 2007, Kavulich Jr 30 et al., 2013, Wang et al., 2013, Wang and Toigo, 2016), and the response of 31 these waves to moderate and large sized dust storms (Basu et al., 2006, 32 Kuroda et al., 2007, Wang and Toigo, 2016), but with only a secondary focus 33 on the pause itself. Most recently, however, Mulholland et al. (2016) used the 34 UK/LMD Mars GCM with both dust and ice radiative forcing to examine 35 the mechanisms of the pause in detail, highlighting the role of both aerosols 36 in modifying the thermal and wind structure at the soltices and in driving the 37 transition of the dominant wavelegths and the amplitudes of trasient waves. 38 In this paper, we examine the solsticial pause in simulations of the Mars 30 Weather Research and Forecasting (MarsWRF) GCM (Richardson et al., 40 2007) using a new dust and water ice microphysics scheme. Two groups 41 of simulations are considered. In the first group ('dry'), dust storms are 42 simulated using a two–moment microphysics scheme and are allowed to de-43 velop spontaneously in the GCM within a dry atmosphere with no surface 44 or atmospheric water but freely evolving atmospheric dust simulated by the 45 model. In the second group of simulations ('wet'), water vapour and ice 46 are included, and heterogeneous nucleation and condensation processes are 47 allowed to produce a self consistent dust and water cycle. To examine the 48 strength (or *depth*) of the solsticial pause, we examine three simulations with 49 each of the wet and dry GCMs with different dust and water cycles (driven by 50

different dust lifting and nucleation rates), with the dustiest model regularly exhibiting a type of northern winter dust storm found only infrequently in the observational record, and the wettest model exceeding typical observations of the water content of present day Mars. All of the simulations shown use a fully interactive dust and water ice (when present) scheme allowing realistic feedback, and produce stable simulations over decadal timescales.

In section 2 we review the GCM configuration and describe the new microphysics scheme. In section 3 we describe the analysis method used to extract the diagnostics of solsticial pause depth, Eady growth rates, and atmospheric energy conversions. In section 4 the results of the simulations are presented and the diagnostics calculated, and in section 5 our interpretation of those results are discussed. Finally, in section 6 the summary of the simulations and our conclusions are provided.

#### <sup>64</sup> 2. Model Description

In this study, we use the MarsWRF GCM (Richardson et al., 2007, Toigo 65 et al., 2012), which includes a two-stream correlated-k radiative transfer 66 scheme to treat the interaction of radiation with the atmosphere and surface 67 (Mischna et al., 2012), and the Yonsei University boundary layer scheme that 68 treats vertical mixing of heat, momentum, and tracers (Hong et al., 2006). 69 For this study, we also introduce a modified version of a terrestrial cloud mi-70 crophysics scheme (Morrison and Gettelman, 2008) that treats microphysical 71 interactions between atmospheric water and dust. In combination with the 72 radiative transfer and boundary layer schemes, the new microphysical scheme 73 in this version of MarsWRF allows for the simulation of self-consistent ra<sup>75</sup> diative, dynamical, and microphysical interactions between dust, water, and
<sup>76</sup> the thermal and dynamical state of the atmosphere.

## 77 2.1. Two-moment dust scheme

Dust is simulated in the model with a fully prognostic two-moment treat-78 ment implemented within the framework of the Morrison and Gettelman 79 (2008) microphysics scheme. In the two-moment scheme the dust particle 80 size distribution is tracked using the total mass density Q and the total num-81 ber density N of the dust at each grid point in the atmosphere. We retain 82 the choice made in Morrison and Gettelman (2008) to use the gamma  $(\Gamma)$ 83 function to describe the family of possible particle size distributions. For the 84 gamma function, the number density,  $\phi$ , is given as a function of particle 85 diameter, D, by 86

$$\phi(D) = N_0 D^\mu \exp^{-\lambda D},\tag{1}$$

where  $N_0$  is the 'intercept parameter' and  $\lambda$  is the 'slope parameter'. The 87 spectral shape parameter,  $\mu$ , determines the shape of the distribution within 88 the gamma distribution family, and is prescribed in the model. Negative 89 values of  $\mu$  have a shape similar to an exponential decay and can be used to 90 simulate a population with large numbers of small particles and fewer large 91 particles. Positive values of  $\mu$  have a shape similar to normal or log-normal 92 distributions and imply a particle size distribution with a spread of values 93 around a peak value, and the width of the distribution is related to the value 94 of  $\mu$  (Morrison and Gettelman (2008) use a value of  $\mu = 1$  for their Earth 95 microphysics scheme). Using this model we can give expressions for mass 96 density and number density as 97

$$N = m(0), \qquad (2)$$

$$Q = \frac{\pi\rho}{6}m(3) \tag{3}$$

where  $\rho$  is the particle density, and m(p) is the *p*th moment of the gamma distribution calculated as

$$m(p) = \int_0^\infty D^p \phi(D) = \frac{N_0}{\lambda^{\mu+p+1}} \Gamma(\mu+p+1).$$
 (4)

 $\Gamma(n)$  is the integrated gamma function, which obeys the relationship  $\Gamma(n + 1) = n\Gamma(n)$ , and is finite all real numbers except negative integers n (where the integral diverges). For a fixed value of  $\mu$ , the values of N, Q, and  $\rho$  are sufficient to calculate the values of  $N_0$  and  $\lambda$  as

$$\lambda = \left(\frac{\pi\rho N\Gamma(\mu+4)}{6Q\Gamma(\mu+1)}\right)^{\frac{1}{3}},\tag{5}$$

$$N_0 = N \frac{\lambda}{\Gamma(\mu+1)} \tag{6}$$

Similarly, the effective radius of the distribution  $(r_{\rm eff})$  can be calculated from  $\lambda$  and  $\mu$ , and the effective variance  $(v_{\rm eff})$  can be calculated directly from  $\mu$  as

$$r_{\rm eff} = \frac{m(3)}{2m(2)} = \frac{\mu+3}{2\lambda},$$
 (7)

$$v_{\text{eff}} = \frac{1}{\mu+3},\tag{8}$$

 $_{106}$   $\,$  and the mass and number density can be related using  $r_{\rm eff}$  as

$$Q = N \frac{4\pi \rho r_{\rm eff}^3}{3} \frac{(\mu+2)(\mu+1)}{(\mu+3)^2}.$$
(9)

Within the atmosphere, dust is affected by both dynamical and micro physical processes. Dynamical processes, including advection and diffusion,

are treated entirely within the two-moment framework by advecting and diffusing Q and N as independent tracers. Sedimentation also occurs in the two-moment framework, with sedimentation velocities calculated for Q and N to appropriately reflect the sedimentation rates of different particle sizes and densities (Morrison and Gettelman, 2008). For a single particle size the sedimentation rate is determined by the Stokes-Cunningham velocity

$$V = \frac{\rho g}{18\eta} D^2 (1 + K(A + Be^{-\frac{E}{K}})), \tag{10}$$

where  $\eta$  is the air viscosity, and  $K = \frac{2\lambda_f}{D}$  is the Knudsen number, given the mean free path,  $\lambda_f$ . Values of A, B and E used in the model are 1.25, 0.43, and 0.95, respectively (Kasten, 1968). This sedimentation rate can be integrated over the particle distribution to determine an appropriately weighted mean fall speed of the number density  $(V_N)$  and mass density  $(V_Q)$ ,

$$V_{N} = \frac{1}{N} \int_{0}^{\infty} V\phi(D)dD, \qquad (11)$$

$$= \frac{\rho g(\mu+1)}{18\eta\lambda} \left( \frac{\mu+2}{\lambda} + 2A\lambda_{f} + \frac{2B\lambda_{f}}{\left(1 + \frac{E}{2\lambda_{f}\lambda}\right)^{\mu+2}} \right), \qquad (12)$$

$$V_{Q} = \frac{1}{Q} \int_{0}^{\infty} V \frac{\pi\rho D^{3}}{6} \phi(D)dD \qquad (12)$$

$$= \frac{\rho g(\mu+4)}{18\eta\lambda} \left( \frac{\mu+5}{\lambda} + 2A\lambda_{f} + \frac{2B\lambda_{f}}{\left(1 + \frac{E}{2\lambda_{f}\lambda}\right)^{\mu+5}} \right).$$

At the surface, dust lifting into the atmosphere is parameterized by two processes. One represents sub-grid scale thermal convective lifting, which is usually ascribed to dust devil vortices, and the other represents lifting by model-resolved wind stress (Newman et al., 2002, Basu et al., 2004, Kahre et al., 2006). The dust is lifted with a fixed effective radius,  $r_{\text{lifted}}$ . The lifting parameterizations control the mass density lifted and  $r_{\text{lifted}}$  is used to calculate the number density lifted from equation 9

$$\frac{\partial N}{\partial t}\Big|_{\text{lifted}} = \frac{3}{4\pi\rho r_{\text{lifted}}^3} \frac{(\mu+3)^2}{(\mu+2)(\mu+1)} \frac{\partial Q}{\partial t}\Big|_{\text{lifted}}.$$
(13)

<sup>127</sup> Surface dust is stored as mass only with an assumed effective radius that im<sup>128</sup> plies a number density on the surface. In the results discussed here we assume
<sup>129</sup> surface dust to be infinitely abundant and uniformly accessible. MarsWRF
<sup>130</sup> includes the ability to limit the abundance of dust (Newman and Richardson,
<sup>131</sup> 2015) but that option is not enabled here as it is not needed to simulate a
<sup>132</sup> generally realistic water ice and dust cycle.

Dust is allowed to interact with radiation through scattering and absorp-133 tion processes within the MarsWRF correlated-k radiation model (Mischna 134 et al., 2012). To account for variable dust particle sizes, a Mie scattering 135 algorithm is used to calculate the scattering and absorption properties of 136 individual dust particles based on their refractive indices (Wolff and Clancy, 137 2003). For this calculation we calculate scattering and absorption coefficients 138 for 8192 dust particle radii (from 0.01 microns to 500 microns) and for 138 139 wavelength bins (from 0.15 to 250 microns). Using this dataset a 'lookup ta-140 ble' of optical properties is generated using a gamma distribution with fixed 141  $v_{\rm eff}$  and calculating the distribution weighted mean properties for a range of 142  $r_{\rm eff}$  values from 0.1 microns to 100 microns. The lookup table generated by 143 this calculation is used within the model to calculate the most appropriate 144 optical properties depending on the effective radius at each grid point. Ref-145 erence optical properties are also calculated at wavelengths (wavenumbers) 146 of 0.67 microns (14925 cm<sup>-1</sup>), 9.3 microns (1075 cm<sup>-1</sup>), and 12.1 microns 147



Figure 1: Reference extinction values for  $v_{\text{eff}} = 0.25$ . Extinction values are shown as the effective radius for radiative processes as a function of the distribution effective radius for microphysics. Solid lines are for dust particles, dotted lines are for water ice particles

(825 cm<sup>-1</sup>) for diagnostic purposes and comparison with observations from the Mars Global Surveyor (MGS) Thermal Emission Spectrometer (TES). The reference extinction coefficients are shown in Figure 1, plotted as the extinction effective radius  $r_{\text{ext}} = \sqrt{\frac{Q_{\text{ext}}}{\pi}}$ .

The gamma function requires a value for the variable  $\mu$ , which defines 152 the effective variance and hence the shape of the gamma function. For dust 153 particles we choose a value of  $\mu = 1$ , corresponding to  $v_{\text{eff}} = 0.25$ , which 154 is within the range of  $v_{\rm eff}$  values inferred by Wolff et al. (2006) from Mars 155 Exploration Rover observations (0.2-0.8) and by Clancy et al. (2003) based 156 on MGS–TES data (0.1-0.4). Figure 2 shows three distributions using the 157 Gamma function, using a value of  $v_{\text{eff}} = 0.25$  (as used here), a value of  $v_{\text{eff}} =$ 158 0.13 which would provide a Gamma distribution close to the log-normal 159



Figure 2: Gamma and log-normal distributions for the effective radius and variance given in the parentheses of each label. (solid black) gamma function with effective radius of  $r_{\rm eff} = 2\mu m$ , and effective variance of  $v_{\rm eff} = 0.25$ . (dashed grey) Log-normal distribution with  $r_{\rm eff} = 2\mu m$ ,  $v_{\rm eff} = 0.4$ . (dash-dotted red) gamma function with  $r_{\rm eff} = 1\mu m$ ,  $v_{\rm eff} =$ 0.13. (dotted blue) gamma function with  $r_{\rm eff} = 2\mu m$ ,  $v_{\rm eff} = 0.4$ .

distribution used by Madeleine et al. (2011), and a much wider Gamma distribution with negative  $\mu = -0.5$  and hence  $v_{\text{eff}} = 0.4$ . The log-normal distribution from Madeleine et al. (2011) is also shown.

#### 163 2.2. Water ice model

Water ice and vapor are included in the GCM using the two-moment scheme described above. At the surface, water is stored as ice overlying the surface, and the surface radiative properties are modified (using an emissivity of 1.0 and albedo of 0.33) where there is more than 5 g/m<sup>2</sup> of water. No active regolith water processes are included in the version used in this study. Water ice (vapor) can be sublimated from (condensed onto) the lowest layer depending on the relative humidity of the lowest atmospheric layer and drag
speed at the surface interface,

$$\frac{\partial q_{\text{vapor}}}{\partial t} = C_v u^* (q - q_{\text{sat}}), \qquad (14)$$

where q is specific humidity,  $u^*$  is the drag speed at the surface interface, and  $C_v$  is a drag coefficient derived from the boundary layer scheme dynamics within the GCM, and depends on the stability conditions in the boundary layer. Similar equations are used to calculate the thermal fluxes at the surface interface.

Once sublimated, water vapor is transported by dynamical processes in 177 the atmosphere, and can nucleate onto bare dust or condense onto ice covered 178 dust. Nucleation follows the parameterization in Inada (2002) and Prup-179 pacher and Klett (2010) assuming direct vapor deposition from a monomer 180 layer of water molecules onto the dust particles (in contrast to the assump-181 tions made in Montmessin et al. (2002) for surface deposition of a steady state 182 influx of water molecules). Condensation follows standard physical parame-183 terizations (Montmessin et al., 2002, Pruppacher and Klett, 2010, Jacobson, 184 1999) for low concentration volatiles in the Martian atmosphere. In the sim-185 ulations conducted in this study, the nucleation contact parameter used is 186 m = 0.95 unless otherwise specified. 187

This model differs from prior microphysical models in the calculation of nucleation and condensation by using adaptive particle sizes instead of the more common fixed particle sizes (e.g. Montmessin et al., 2002, Navarro et al., 2014). In our model, the bin locations are specified in terms of quantiles (of fixed percentage) of the total distribution independent of modal radius. These bins remain fixed in percentile space (but move in radius space) as the <sup>194</sup> ice particles grow and shrink and are used by the nucleation and condensation <sup>195</sup> processes to calculate the bin-averaged particle properties such as size, mass, <sup>196</sup> and growth rates. Using fixed quantiles rather than fixed radii means that <sup>197</sup> condensation processes are better resolved at larger particle radius instead <sup>198</sup> of performing most condensation calculations for 'large' particles (e.g. those <sup>199</sup> over 10 microns radius) in a single bin.

During nucleation of water vapor onto bare dust, cloud condensation nu-200 clei (CCN) are formed by scavenging (removing) dust particles from the dust 201 population and tracked as independent particles with additional two-moment 202 mass and number tracers that are transported by atmospheric dynamics. The 203 CCN number tracer becomes the number tracer for ice particles that form on 204 the CCN, and a new mass tracer is used to track the mass of ice deposited 205 onto the CCN population. The radius and mean density of the water ice 206 particles (including contributions of ice and dust) are used in the sedimen-207 tation equations 11 and 12 to calculate sedimentation rates for ice particles, 208 allowing the model to properly differentiate ice particles based on radius and 200 mass separately. 210

All microphysical processes occur on the MarsWRF GCM 'dynamics' timestep (3 minutes for a global 5–degree simulation) with no sub–timestepping in the nucleation or condensation processes. Radiative properties are updated during a 'physics' timestep when radiative flux calculations are performed (typically 15 or 30 minutes for a global 5–degree simulation).

Water ice particles that sediment, or are otherwise transported, to the surface are included in the total ice and dust deposits on the surface. In the current model, dust and ice are separated upon contact with the surface and water ice overlays dust. Surface radiative properties at each grid point are altered if there is sufficient water ice on the surface  $(5 g/m^2)$ , or equivalently  $5.4 \mu m$  of surface ice depth). Radiative properties of water ice clouds are calculated using the same method applied to dust, using refractive index data for water ice at 220 K (Iwabuchi and Yang, 2011). Reference extinction coefficients used in generating figures for comparison with TES are shown in Figure 1.

In the simulations discussed here, the effective variance  $(v_{\text{eff}})$  of the water ice distribution is set to the same value as the dust distribution, with a value of 0.25 (see Figure 2). This choice neglects the narrowing of the water ice distribution by condensation (as assumed by Navarro et al. (2014)) and implies that the mean ice particle age is relatively low and the size distribution of ice particles reflects the size distribution of the CCN.

#### 232 2.3. Model setup and experiment cases

To examine the solsticial pause with this new model, each simulation uses 233 the self-consistent dust lifting schemes contained in the GCM to produce a 234 dust cycle appropriate for the thermal and lifting conditions in the GCM. 235 Three simulations are performed with the dry GCM: the first has only low 236 opacity background dust (roughly equivalent in average optical depth to the 237 MGS-MCD scenario of Montmessin et al. (2004) but using only interactive 238 dust processes for its generation), the second has a typical unit opacity ( $\tau$ 239  $\approx$  1) dust storm, and the third simulation has a larger ( $\tau \approx 5$ ) dust storm 240 (dryL, dryM, dryH, respectively). Three simulations are also performed 241 with the wet GCM: the first has typical northern spring and summer ice 242 cloud abundances and unit optical depth dust storms, the second is a low 243

nucleation rate (contact parameter m = 0.9) simulation with higher opacity 244 dust storms and cloud opacities, and the third has a low dust opacity but 245 with water vapor column abundances exceeding those observed on Mars, 246 (wetL, wetM, wetH, respectively). Figure 3 shows the total column opacity 247 at 9.3 microns over the equator for the six simulations used in this paper: 248 By coincidence (rather than by construction) ordering the simulations by 249 peak total opacity is equivalent to ordering the dry models by dust opacity 250 at  $L_s = 300^{\circ}$  (see Figure 4) and the wet models by water ice opacity at 251  $L_s = 150^{\circ}$  (see Figure 5), but the order of the simulations is not preserved 252 in the depth of the solsticial pause. Figure 4 shows the column dust opacity 253 for these simulations for a year of each simulation. Figure 5 shows the water 254 vapour and ice column abundance for the **wet** models only. 255

# <sup>256</sup> 3. Solsticial pause diagnostic

To examine the extent and strength of the solsticial pause we implement 257 a version of the diagnostic developed by Lewis et al. (2016) and Mulholland 258 et al. (2016), where the pause is characterized by the medium-term tem-259 perature variability of the winter atmosphere. Specifically, we perform five 260 processing steps: the first two follow Lewis et al. (2016), the third and fourth 261 follow Mulholland et al. (2016) in the generation of a useful metric of pre-262 solstice and during-solstice atmospheric variability, and finally, we slightly 263 modify a diagnostic developed by Mulholland et al. (2016) that provides a 264 single-valued gauge of the 'depth' of the solsticial pause for a given simula-265 tion. Specifically we perform the following calculations: 266

<sup>267</sup> 1. The air temperature on a level 2.5 km above the surface is sampled at



Figure 3: Total column opacity over the equator at 9.3 microns for the six simulations. Data shown in opacity/optical depth units, for the 25th year of each simulation, sampled every 3 hours and averaged into 5–sol periods. The colors used in this figure are used in other figures in this paper to identify the same model where necessary.



Figure 4: Dust column opacity at 9.3 microns for the six simulations. Wet simulations shown on the top row are (from left to right) wetL, wetM, wetH. Dry simulations are shown on the bottom row (from left to right) dryL, dryM, dryH. Contours shown in opacity units, for the 25th year of each simulation, sampled every 3 hours and averaged into 5 sol periods. The colors used in the sub-plot titles in this figure are used to identify the same simulation in other figures and also correspond to the colors used in the curves in figure 3 and 10.



Figure 5: Water ice and vapour for the wet models only. Water ice column opacity at 11.9 microns shown on the top row from simulations (left to right) **wetL**, **wetM**, **wetH**. The bottom row shows water vapour column abundance in precipitable microns for each simulation.

<sup>268</sup> 3 hourly intervals and is filtered using a Butterworth (1930) band-pass
<sup>269</sup> filter to retain waves with periods of 1.5 to 30 sols. Figure 6 shows an
<sup>270</sup> example pressure cycle for this GCM, the Butterworth filter shape as
<sup>271</sup> a function of time, and the resulting bandpass filtered dataset.

272 2. The standard deviation of the filtered temperature is calculated using
a 30-sol sliding window, and treated as the atmospheric variability.

3. The domain-maximum value of atmospheric variability is calculated
for each time sample in the domain from 30-80° latitude in the winter
hemisphere.

4. The time-averaged domain-maximum variability is calculated for two time periods. (A) Within 30° of solstice, and (B) the 180° period surrounding solstice but not including period 'A'. For southern winter region A is  $L_s = 60-120^\circ$ , region B is  $L_s = 0-60^\circ$  and  $L_s = 120-180^\circ$ . For northern winter region A is  $L_s = 240 - 300^\circ$ , region B is  $L_s =$  $180 - 240^\circ$  and  $L_s = 300 - 360^\circ$ .

5. We define the solsticial pause depth as  $100\% \times (1 - \frac{A}{B})$  where A and B 283 are the domain averaged values defined above. Larger positive values 284 describe a larger relative decrease in wave activity, *i.e.* a deeper solsti-285 cial pause is represented by a larger percentage depth up to a complete 286 cessation of solsticial variance for a depth of 100%. A zero value would 287 suggest no solsticial pause, while negative values describe an increase 288 in wave activity during the solstice. The ratio A/B used by Mulholland 289 et al. (2016) is slightly less intuitive as a gauge of the depth. 290

For comparison with observations we use the MACDA reanalysis of the MGS TES observations as presented with a specific focus on the solsticial



Figure 6: (left) Butterworth band-pass filter (grey) and low-pass filter (black) shown in frequency units. The horizontal dashed line shows the 3 dB drop-off for the filters (where the power would be reduced to 50% of its original value). (top right) Surface pressure data at 70 °N from the **dryM** model (grey) and low-pass filtered data (black) using the low pass filter shown on the left. (bottom right) band-pass filtered pressure data from the same dataset.

pause by Lewis et al. (2016). As in Earth climate studies (e.g. Kalnay et al., 293 1996) we treat this 'reanalysis dataset' as a proxy for real observational data 294 of the Mars atmosphere. Lewis et al. (2016) provides figures (particularly 295 their figure 1) showing the absolute amplitude of wave activity using similar 296 post-processing methods to those described in this paper. The MACDA 297 reanalysis is also examined by Wang and Toigo (2016), who show the seasonal 298 cycle of the zonal wavenumber 1 to 3 eastward traveling transient waves at 299 low and middle atmospheric levels for the northern hemisphere. 300

We undertake detailed comparisons with two recent free-run Mars GCM 301 studies of the solsticial pause. Mulholland et al. (2016) use the UK/LMD 302 MGCM with prescribed dust optical depth but an otherwise freely evolving 303 simulation including water ice and dust. The paper provides explicit quanti-304 tative diagnostics for their simulations which we reproduce for comparison. 305 Wang and Toigo (2016) use the MarsWRF GCM to perform simulations 306 with highly idealized dust opacity (Montmessin et al., 2004) with ad-hoc 307 wave forcing to induce wavenumber 3 activity during the southern summer 308 dust storms. While they do not explicitly calculate a solsticial pause diag-300 nostic, they do use output from these simulations to calculate the amplitude 310 of waves and energy transfers during the solstice periods. 311

# 312 4. Results

Figure 7 shows the variability of the air temperature at  $\approx 2.5$  km altitude for waves with a period of 1.5 to 30 sols for each of the six simulations. This dataset is used to calculate the solsticial pause depth given in Tables 1 and 2. This figure shows a large decrease in northern hemisphere atmospheric variability around  $L_s = 270^{\circ}$  in all wet and two dry models, and a smaller decrease in the dry model with lowest dust opacity (**dryL**). The wet models also have a decrease in the southern hemisphere variability around  $L_s = 90^{\circ}$ while the dry models have a small decrease or increase during the same time period.

For the dry simulations, the depth of the solsticial pause is directly related 322 to the magnitude of the perihelion dust storm, with stronger storms and 323 deeper pauses occurring in the same simulation. The absolute variability 324  $(T'_{\rm max})$  is also dependent on the dust opacity; higher dust opacity corresponds 325 to lower absolute temperature variability. In the southern winter in these 326 dry simulations, the lack of significant opacity from dust or water ice clouds 327 results in a consistent polar variability across the simulations regardless of 328 peak dust opacity, and with little or no pause in wave activity. 329

In the wet models the relationship between atmospheric opacity and the 330 solsticial pause depth is similar to the dry models, if we consider the total 331 opacity from the dust and water ice particles. The southern winter pause 332 depth is dependent on the structure and opacity of the polar ice clouds (see 333 Table 2), which varies between the wet simulations. In northern winter the 334 water ice opacity dominates along the edge of the polar night-time (where 335 the solsticial pause is strongest) and is relatively consistent between each 336 simulation as it is controlled more by the presence of water vapor and ice 337 along the polar terminator than the equatorial dust storms. As a result, all 338 three simulations have a pause depth of around 40% and  $T'_{\rm max}$  values during 339 northern winter solstice of around 3.5K, both values in agreement with values 340 calculated by Mulholland et al. (2016) for the MACDA reanalysis dataset 341

 $_{342}$  (Lewis et al., 2016).

The northern winter solsticial pauses produced in the wet simulations are 343 deeper than the pauses reported in Mulholland et al. (2016), and although 344 Wang and Toigo (2016) do not calculate the same diagnostic, their results 345 are qualitatively comparable to those produced here for the **dryL** simulation. 346 The wet simulations here are closer to the reanalysis results from Lewis et al. 347 (2016) than the free-run simulations from Mulholland et al. (2016). All three 348 wet simulations also have a solsticial pause during the southern winter season 349 (around  $L_s = 90^\circ$ ) along the edge of the southern polar cap instead of the 350 northern cap. The absolute values of  $T'_{\rm max}$  found in the wet simulations are 351 in good agreement with the reanalysis dataset shown in figure 1 of Lewis 352 et al. (2016). 353

# 354 4.1. Eady Growth rates

Mulholland et al. (2016) analyzed the solsticial pause in a number of GCM simulations using the UK/LMD GCM that forms the basis of the MACDA reanalysis product (Lewis et al., 2016). In Mulholland et al. (2016), the stability of the atmosphere around winter solstice was studied using the Eady growth rate as a measure of the baroclinic stability of the lower atmosphere. The Eady growth rate (Vallis, 2006) is given by

$$\sigma = 0.31 \frac{f}{N} \frac{\partial \overline{u}}{\partial z} \tag{15}$$

for a Coriolis parameter f, static stability N, and vertical shear of horizontal wind  $\frac{\partial \overline{u}}{\partial z}$ . High values of  $\sigma$  correspond to large growth rates and a baroclinically unstable atmosphere, making it more likely that baroclinic waves



Figure 7: Magnitude of medium-term variability in the lower atmosphere. Calculated as the 30-sol running standard deviation of temperature waves at 2.5km altitude, filtered for waves with periods between 1.5 to 30 sols. Layout as Figure 4, units of K.

Simulation	$T'_{\rm max}$ solstice (K)	$T'_{\rm max}$ surrounding (K)	Pause depth $(\%)$
dryL	6.84	8.32	18
dryM	4.21	6.86	39
dryH	2.14	5.24	59
$\mathbf{wetL}$	3.70	6.07	39
wetM	3.36	5.88	43
wetH	3.55	6.37	44
MACDA	3.35	6.72	50
$ au_{\mathbf{MY24}}$	6.40	7.09	10
$ au^*_{\mathbf{MY24}}$	5.55	7.94	30
$\tau_{\mathbf{low}}$	7.91	7.42	-7
$ au^*_{\mathbf{low}}$	8.39	9.18	9
$ au_{\mathbf{high}}$	5.51	7.27	24

Table 1: Average value of meridional domain-maximum  $(30^{\circ} - 80^{\circ} \text{ latitude})$  variability and solsticial pause depth.  $T'_{\text{max}}$  values are calculated as the seasonal average of meridional maximum standard deviation of 1.5–30 sol period temperature waves at 2.5km altitude, in units of Kelvin. Pause depth in units of percent. The solstice is defined as  $L_s = 270^{\circ} \pm 30^{\circ}$ and surrounding seasons encompassing  $L_s = 180^{\circ} - 360^{\circ}$  excluding the solstice period. Top five rows are from the MarsWRF GCM used in this study (see text for simulation label definitions). MACDA values are taken from reanalysis data (Lewis et al., 2016) as presented by Mulholland et al. (2016). Bottom five rows correspond to simulations from the UK/LMD MGCM by Mulholland et al. (2016) using the simulation labels from that paper.

Simulation	$T'_{\rm max}$ solstice (K)	$T'_{\rm max}$ surrounding (K)	Pause depth (%)
dryL	3.08	3.50	12
dryM	3.08	3.28	6.3
dryH	3.06	3.04	-0.5
$\mathbf{wetL}$	2.00	3.94	49
wetM	2.49	3.79	34
$\operatorname{wetH}$	1.43	3.85	63

Table 2: As Table 1, but for the southern hemisphere, with solstice defined as  $L_s = 90^{\circ} \pm 30^{\circ}$  and surrounding seasons encompassing  $L_s = 0^{\circ} - 180^{\circ}$  excluding the solstice periods.

would be generated, while low values of  $\sigma$  correspond to a more baroclin-364 ically stable atmosphere, with eddy generation possibly due to barotropic 365 eddy generation instead (Deng and Mak, 2006). For the free-run simulations 366 and reanalysis dataset in Mulholland et al. (2016) the Eady growth rate was 367 found to decrease during the solsticial pause, a signature of increasing baro-368 clinic stability. Figure 8 shows the value of the Eady growth rate for each 369 simulation in the Northern hemisphere for the half of the Martian year that 370 includes northern winter solstice  $(L_s = 180^{\circ} - 360^{\circ}).$ 371

The eddy temperature field in Figure 8 shows the domain-maximum values of the results in Figure 7 (i.e. maximum value between 30°N and 80°N as a function of time) and in each case shows a distinct depression corresponding to the solsticial pause in that simulation. In the dry models, the pause structure is essentially uni-modal, while the dustier wet models have a weak bi-modal structure with a local maximum occurring around  $L_s = 315^\circ$ . The wet models also appear to have more consistent variability across the simu-



Figure 8: Eady growth rates and eddy temperature fields as a function of  $L_s$  for each simulation. Layout as Figure 4. black: Eddy temperature field (K) at 2.5 km altitude, meridional domain maximum at each time. red: Eady growth rate  $(s^{-1})$  at 200 m and at the latitude of maximum eddy temperature (shown in black), blue: meridional domain maximum Eady growth rate  $(s^{-1})$  at 200 m.

lations during the  $L_s = 180^{\circ}-225^{\circ}$  period and consistent timing of minimum variability near Ls=270°. In contrast, the dry models have variation in the amplitude of the maximum variability and timing of the minimum depending on the dust opacity.

In the dry simulations there is a weak correlation between the eddy tem-383 perature field and the Eady growth rates at the latitude of the eddy tem-384 perature field maximum (i.e. red and black lines). Further, for the dryL 385 simulation the domain maximum Eady growth rate (blue line) remains rela-386 tively high and lacks a substantial pause. This result is in line with results 387 shown in Mulholland et al. (2016), and suggests that in the dry simulations 388 the observed eddies (in temperature) are influenced by eddies generated fur-389 ther poleward that propagate into the mid-latitudes and maintain the eddy 390 temperature field there. 391

The wet simulations have no obvious correlation between the Eady growth rates and the temperature field. All three simulations have similar Eady growth rates during solstice and the region of maximum instability in these simulations (where Eady growth rates are maximized) is further removed from the maximum variability, except toward the end of the winter after  $L_s = 330^\circ$  where the eddy amplitude peak moves poleward as shown in Figure 12 later.

# 399 4.2. Energy transfers

An alternative diagnostic of baroclinic activity was used by Wang and Toigo (2016), who studied wave activity in the MarsWRF GCM using an ad-hoc forcing to simulate a travelling wavenumber 3 mode in the winter atmosphere. Using Fourier decomposition, they found a northern winter

solsticial pause and used energy diagnostics to investigate the relative contri-404 butions of baroclinic and barotropic processes using the methodology derived 405 in Ulbrich and Speth (1991). In Ulbrich and Speth (1991) the atmosphere is 406 partitioned into four reservoirs (with a further 4 sub-reservoirs not used here) 407 - the mean available potential energy (AZ), eddy available potential energy 408 (AE), mean kinetic energy (KZ), and eddy kinetic energy (KE). The direc-409 tion and magnitude of energy transfers between these reservoirs can be used 410 as a diagnostic for instability processes in the atmosphere. In particular, 411 baroclinic processes transfer energy along  $AZ \rightarrow AE \rightarrow KE$ , while barotropic 412 processes transfer energy along  $AZ \rightarrow KZ$ . 413

Figure 9 shows the calculated energy transfers for the entire year for a re-414 gion between 50 and 70 degrees north, and 1km to 20km altitude. These plots 415 highlight the different route through which energy is transferred in each sim-416 ulation. In the dry models, the energy transfer through baroclinic processes 417  $(AZ \rightarrow AE)$  is relatively consistent throughout the winter, with barotropic 418 processes  $(AZ \rightarrow KZ)$  increasing before solstice and decreasing after it. In-410 creased dust loading corresponds to increased barotropic energy transfer in 420 these simulations, and less consistent baroclinic energy transfer. In the wet 421 models the solsticial pause effect is stronger because of two effects - baroclinic 422 processes  $(AZ \rightarrow AE)$  that dominate away from the solstice rapidly dissipate 423 prior to the solution, while barotropic processes  $(AZ \rightarrow KZ)$  increase prior to 424 the solstice, as in the dry model. The combination of the two processes pro-425 duces a more defined pause structure in the wet simulations than in the dry 426 simulations. This difference is also present in the energy reservoirs themselves 427 (not shown): where the dry simulations retain much of the eddy energy (AE 428



Figure 9: Energy transfer between 50°N and 70°N from 1km to 20km altitude. blue: AZ $\rightarrow$ KZ, green: AE $\rightarrow$ KE, red: KZ $\rightarrow$ KE, magenta: AZ $\rightarrow$ AE. Units of  $W/m^2$ .

and KE) throughout the northern winter, the wet simulations tend to lose
eddy energy in favour of zonal mean energy (KZ, in particular).

In the polar region, the transition from baroclinic energy transfers to 431 barotropic energy transfers is driven by a change in the wind and temper-432 ature structure in the lower atmosphere, which is partly controlled by the 433 optical depth of aerosols in the atmosphere. Figure 10 shows the vertical 434 gradient of mean horizontal wind and mean temperature profile for the low-435 est 20km of the atmosphere between  $50^{\circ}$ N and  $70^{\circ}$ N, and for periods before, 436 during, and after the solstice. The structural change in the wet simulations 437 occurs as the wind gradients  $\left(\frac{\partial \overline{u}}{\partial z}\right)$  decrease substantially (and almost disap-438 pear near the surface) during the pause, reducing the baroclinic growth rate 439 (equation 15). In the dry models, the structural change is more visible in 440



Figure 10: Thermal and wind structure in the lower atmosphere, averaged over  $50 - 70^{\circ}$ N, for the periods (left)  $L_s = 210 - 230^{\circ}$ , (center)  $L_s = 260 - 280^{\circ}$ , (right)  $L_s = 310 - 0^{\circ}$ . (top row) Vertical gradient of zonal (west-east) wind, units of (m/s)/km. (bottom row) mean temperature, units of K. orange: **dryL**, purple: **dryM**, yellow: **dryH**, blue: **wetL**, green: **wetM**, red: **wetH**.

the thermal structure, where changes in the temperature profile increase the static stability (N) of the atmosphere and inhibit baroclinic eddy growth.

## 443 5. Discussion

From the eddy amplitude plots (Figure 7), it is clear that the pause depth and extent are stronger in simulations with water in the atmosphere than dry simulations, except in simulations with exceptionally large dust storms. In addition, the presence of water greatly stabilizes the northern hemisphere  $L_s = 270^\circ$  pause and allows a southern hemisphere  $L_s = 90^\circ$  pause to form within the same simulation.

For the  $L_s = 270^{\circ}$  pause, the wet simulations tend to produce a pause 450 amplitude and depth that is relatively insensitive to the dust and water ice 451 abundance and agrees well with the MACDA reanalysis results (Lewis et al., 452 2016). The wet simulations conducted here are generally in better agreement 453 with the MACDA reanalysis than the the UK/LMD GCM (Mulholland et al., 454 2016), and, in general, MarsWRF tends to produce deeper solsticial pauses 455 even in dry simulations, as shown here and in Wang et al. (2013) for simpler 456 dust configurations. 457

The depth of the pause varies between simulations, and has a good cor-458 relation with the total opacity near the polar cap edge during the winter 459 solstice. For the northern winter solstice the opacity is provided by a large 460 dust storm in wet and dry simulations, and by ice clouds along the polar 461 terminator in the wet simulations. For the southern winter solstice the dust 462 opacity is consistently low across all simulations and the opacity comes from 463 ice clouds along the equator and along the southern polar terminator (peak-464 ing at about  $45^{\circ}$  latitude in both winter hemispheres). Figure 11 shows the 465 opacity from each aerosol as a function of latitude for 30 degrees around each 466 solstice. 467

Decomposing the energy reservoirs by longitudinal wavenumber we find that the wet models have a more complex evolution of eddy activity during the northern fall season which might contribute to the enhanced solsticial pause (Figure 12). Wavenumber 1 modes dominate as the polar cap forms, with a transition to higher wavenumber (2–4) modes later in the season before the solsticial pause. After the pause the opposite trend occurs as the ice cap sublimates and polar night retreats poleward. Note that because



Figure 11: Opacity at 9.3 microns as a function of latitude for  $30^{\circ}$  of  $L_s$  around the southern winter solstice ( $L_s = 90^{\circ}$ , top) and the northern winter solstice ( $L_s = 270^{\circ}$ , bottom). The plots show (from left to right) the total aerosol opacity, dust opacity, and water ice opacity. As in Figure 3 the colors identify the simulation, wetL (blue), wetM (green), wetH (red), dryL (orange), dryM (purple), dryH (yellow).



Figure 12: Available Eddy Potential Energy in wavenumber 1–4 (left to right) for wetL (top row) and dryM (bottom) simulations. Contour levels for wavenumber 1 are scaled down by a factor of 2. Units of  $J/m^2$ . The horizontal axis has been shifted in these plots to place  $L_s = 270^{\circ}$  at the center of each plot.

MarsWRF is a grid model, the polar points are subject to numerical filtering
to ensure stability; however, global wavenumbers 1–4 are not substantially
filtered equatorward of 82.5° latitude and do not impact the results here.

In the dry simulations there is an enhancement of the wavenumber 2 478 mode, but with a distinct lack of energy in the other cap edge modes. This 479 wavenumber 2 mode occurs at the same time and location as the pre-pause 480 enhancement of temperature variability in the dry simulations. In the dusti-481 est dry simulation (**dryH**) there is an additional wavenumber 2 enhance-482 ment over the equator during the peak of the storm, which alters the energy 483 balance in the equatorial region and extra-tropics but doesn't contribute 484 significantly to the polar solsticial atmosphere (the oscillation in  $KZ \rightarrow KE$ 485 in dryH around  $L_s = 300^{\circ}$  shown in Figure 9 is related to this equatorial 486 enhancement). 487

As Mulholland et al. (2016) noted, the presence of dust and ice in the 488 atmosphere alters the near-surface thermal structure near the polar cap and 489 reduces the vertical wind shear that drives baroclinic processes in this re-490 gion. Calculations of baroclinic instability (Mulholland et al., 2016) and 491 energy conversion diagnostics (Wang and Toigo, 2016) tend to suggest that 492 baroclinic energy conversion decreases during solstice and barotropic energy 493 conversion increases to produce the observed pause in eddy activity, in favour 494 of faster zonal mean winds. 495

### 496 6. Conclusions

A new version of the MarsWRF GCM with radiative-dynamical-microphysical 497 feedbacks was used to simulate a range of dust and ice conditions to exam-498 ine the sensitivity of the solsticial pause. In dry simulations MarsWRF will 499 produce a northern winter solsticial pause if a sufficiently large dust storm 500 is present, but the dust storm peak opacity needed to reproduce the reanal-501 vsis results is larger than typically observed on Mars (with peak opacities 502 of 0.5-1), while the pause is observed to occur in the Martian atmosphere 503 during years with and without large dust storms (Lewis et al., 2016). The 504 dry simulations also do not produce a southern summer solsticial pause. In 505 wet simulations MarsWRF produces solsticial pauses in both winter hemi-506 spheres, and with a pause depth that is in good agreement with the absolute 507 and relative pause magnitude in the MACDA reanalysis dataset. In all of 508 the simulations conducted, the depth of the solsticial pause is related to the 509 total column aerosol opacity but with a non-linear dependence because of 510 the different spatial and temporal behaviour of dust storms and cap-edge ice 511

clouds. The typical wet simulations (wetL and wetM) produce solsticial
pause depths in both hemispheres that agree well in absolute and relative
magnitudes with the MACDA reanalysis.

The solsticial pause occurs in the MarsWRF simulations as baroclinic 515 instabilities that dominate away from the solstice are inhibited during the 516 solstice, allowing an increase in barotropic energy conversion. In dry simu-517 lations the inhibition is due to changes in the thermal structure of the lower 518 atmosphere caused by lower latitude dust storms. In wet simulations the 519 inhibition is due to changes in the local opacity due to ice clouds that re-520 duces the near surface wind shear. Both processes lead to a reduction in 521 baroclinic instability growth. The processes generating the pause in Mar-522 sWRF with interactive dust and cloud ice are similar to those reported from 523 examination of the MACDA reanalysis data (Lewis et al., 2016), and from 524 previous modeling with the UK/LMD MGCM (Mulholland et al., 2016) and 525 with prescribed dust opacity in MarsWRF (Wang and Toigo, 2016). 526

The much improved simulation of the solution pause with the present 527 version of MarsWRF is due to the addition of a newly developed dust-ice 528 microphysics model. The model uses a hybrid scheme combining efficient 529 two-moment tracers to simulate dynamic processes and accurate adaptive-530 binned microphysics to simulate nucleation and condensation. Five atmo-531 spheric tracers are used to track the evolution of dust mass density, dust 532 number density, water ice mass density, water ice and CCN number den-533 sity, and CCN mass. The microphysics model allows the radiative forcing of 534 MarsWRF to evolve more realistically as dust and cloud ice abundance and 535 particle size distributions evolve under the influence of interactive dust lift-536

<sup>537</sup> ing from the surface, resolved and un-resolved mixing within the atmosphere, <sup>538</sup> microphysical interactions between dust, water, and the atmospheric thermal <sup>539</sup> state, and particle-size-dependent sedimentation. The model results confirm <sup>540</sup> the importance of ice radiative effects for the development of the winter sol-<sup>541</sup> sticial pause (Mulholland et al., 2016) and for the atmospheric thermal and <sup>542</sup> dynamical state of Mars more generally (Wilson et al., 2007).

# 543 Acknowledgement

Funding for this work were provided by the NASA Mars Fundamental Research Program grant NNX13AK67G and the University of Toronto. Resources supporting this work were provided by the NASA High-End Computing (HEC) Program through the NASA Advanced Supercomputing (NAS) Division at Ames Research Center. A portion of this research was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration.

# 551 7. References

- D. Banfield, B. Conrath, P. Gierasch, R. J. Wilson, and M. Smith. Traveling
  waves in the martian atmosphere from mgs tes nadir data. *Icarus*, 170(2):
  365–403, 2004.
- J. R. Barnes, J. B. Pollack, R. M. Haberle, C. B. Leovy, R. W. Zurek, H. Lee,
  and J. Schaeffer. Mars atmospheric dynamics as simulated by the nasa
  ames general circulation model: 2. transient baroclinic eddies. *Journal of Geophysical Research: Planets*, 98(E2):3125–3148, 1993.
- S. Basu, M. I. Richardson, and R. J. Wilson. Simulation of the Martian dust cycle with the GFDL Mars GCM. Journal of Geophysical Research, 109(E11):1-25, 2004. ISSN 0148-0227. doi: 10.1029/2004JE002243.
  URL http://www.agu.org/pubs/crossref/2004/2004JE002243.shtml http://doi.wiley.com/10.1029/2004JE002243.
- S. Basu, J. Wilson, M. Richardson, and A. Ingersoll. Simulation of spontaneous and variable global dust storms with the GFDL Mars GCM. *Journal*of Geophysical Research E: Planets, 111(9):1–33, 2006. ISSN 01480227. doi:
  10.1029/2005JE002660.
- S. Butterworth. On the Theory of Filter Amplifiers. Wireless Engineer, 7:
   536–541, 1930.
- <sup>570</sup> R. T. Clancy, M. J. Wolff, and P. R. Christensen. Mars aerosol
  <sup>571</sup> studies with the MGS TES emission phase function observations:
  <sup>572</sup> Optical depths, particle sizes, and ice cloud types versus lati<sup>573</sup> tude and solar longitude. *Journal of Geophysical Research*, 108

(E9), 2003. ISSN 0148-0227. doi: 10.1029/2003JE002058. URL
 http://www.agu.org/pubs/crossref/2003/2003JE002058.shtml.

- <sup>576</sup> M. Collins, S. Lewis, P. Read, and F. Hourdin. Baroclinic wave transitions <sup>577</sup> in the martian atmosphere. *Icarus*, 120(2):344–357, 1996.
- Y. Deng and M. Mak. Nature of the Differences in the Intrasea-578 sonal Variability of the Pacific and Atlantic Storm Tracks: A Di-579 agnostic Study. Journal of the Atmospheric Sciences, 63(10):2602-580 2615, 2006. ISSN 0022-4928. 10.1175/JAS3749.1. URL doi: 581 http://journals.ametsoc.org/doi/abs/10.1175/JAS3749.1. 582
- S. D. Guzewich, A. D. Toigo, L. Kulowski, and H. Wang. Mars orbiter camera
  climatology of textured dust storms. *Icarus*, 258:1–13, 2015.
- Y. Noh, S. Y. Hong, and J. Dudhia. А new vertical dif-585 fusion package with an explicit treatment of entrainment pro-586 Monthly Weather Review, 134:2318–2341, 2006.URL cesses. 587 http://journals.ametsoc.org/doi/abs/10.1175/MWR3199.1. 588
- A. Inada. Numerical simulations of Martian fog formation and inflight calibration of Mars imaging camera on NOZOMI for its future observations.
   PhD thesis, Kobe University, 2002.
- H. Iwabuchi and P. Yang. Temperature dependence of ice optical constants: Implications for simulating the single-scattering properties of cold ice clouds. Journal of Quantitative Spectroscopy and Radiative Transfer, 112(15):2520-2525, 2011. ISSN 00224073. doi: 10.1016/j.jqsrt.2011.06.017.
  URL http://dx.doi.org/10.1016/j.jqsrt.2011.06.017.

- M. Z. Jacobson. Fundamentals of Atmospheric Modeling. Cambridge Uni versity Press, 1999.
- M. A. Kahre, J. R. Murphy, and R. M. Haberle. Modelling the Martian dust
  cycle and surface dust reservoirs with the NASA Ames general circulation
  model. *Journal of Geophysical Research E: Planets*, 111(6):1–25, 2006.
  ISSN 01480227. doi: 10.1029/2005JE002588.
- E. Kalnay, M. Kanamitsu, R. Kistler, W. Collins, D. Deaven, L. Gandin,
  M. Iredell, S. Saha, G. White, J. Woollen, Y. Zhu, A. Leetmaa,
  R. Reynolds, M. Chelliah, W. Ebisuzaki, W. Higgins, J. Janowiak, K. C.
  Mo, C. Ropelewski, J. Wang, R. Jenne, and D. Joseph. The NCEP/NCAR
  40-Year Reanalysis Project. *Bulletin of the American Meteorological So- ciety*, 77(3):437–471, mar 1996. ISSN 0003-0007. doi: 10.1175/15200477(1996)077j0437:TNYRPj2.0.CO;2.
- F. Kasten. Falling Speed of Aerosol Particles. Journal of Applied Meteorology,
  7:944–947, 1968. ISSN 0894-8763.
- M. J. Kavulich Jr, I. Szunyogh, G. Gyarmati, and R. J. Wilson. Local
  dynamics of baroclinic waves in the martian atmosphere. *Journal of the Atmospheric Sciences*, 70(11):3415–3447, 2013.
- T. Kuroda, A. S. Medvedev, P. Hartogh, and M. Takahashi. Seasonal changes
  of the baroclinic wave activity in the northern hemisphere of mars simulated with a gcm. *Geophysical research letters*, 34(9), 2007.
- Ρ. Mulholland, Ρ. L. S. R. Lewis, D. L. Read. Montabone. 618 J. Wilson, M. D. Smith. The solsticial pause on R. and 619

Mars: A planetary 264:456-464.1. wave reanalysis. Icarus, 620 2016.ISSN 10902643. 10.1016/j.icarus.2015.08.039. URL doi: 621 http://dx.doi.org/10.1016/j.icarus.2015.08.039. 622

J. B. Madeleine, F. Forget, E. Millour, L. Montabone, and M. J. Wolff.
Revisiting the radiative impact of dust on Mars using the LMD Global
Climate Model. *Journal of Geophysical Research E: Planets*, 116(11):1–
13, 2011. ISSN 01480227. doi: 10.1029/2011JE003855.

M. A. Mischna, C. Lee, and M. I. Richardson. Development of a fast, accurate
radiative transfer model for the Martian atmosphere, past and present. *Journal of Geophysical Research*, 117(E10):E10009, oct 2012. ISSN 01480227. doi: 10.1029/2012JE004110.

- L. Montabone, K. Marsh, S. Lewis, P. Read, M. Smith, J. Holmes, A. Spiga,
  D. Lowe, and A. Pamment. The mars analysis correction data assimilation
  (macda) dataset v1. 0. *Geoscience Data Journal*, 1(2):129–139, 2014.
- F. Montmessin, P. Rannou, and M. Cabine. New insights into Martian dust
  distribution and water-ice cloud microphysics. *Journal of Geophysical Re- search*, 107(E6):5037, 2002. ISSN 0148-0227. doi: 10.1029/2001JE001520.
  URL http://doi.wiley.com/10.1029/2001JE001520.

F. Montmessin, F. Forget, P. Rannou, M. Cabane, and R. M. Haberle. Origin and role of water ice clouds in the Martian water cycle as inferred from a general circulation model. *Journal of Geophysical Research*, 109 (E10):1-26, 2004. ISSN 0148-0227. doi: 10.1029/2004JE002284. URL http://www.agu.org/pubs/crossref/2004/2004JE002284.shtml.

H. Morrison and A. Gettelman. A new two-moment bulk stratiform cloud microphysics scheme in the community atmosphere model, version 3 (CAM3).
Part I: Description and numerical tests. *Journal of Climate*, 21(15):3642–
3659, 2008. ISSN 08948755. doi: 10.1175/2008JCLI2105.1.

- D. P. Mulholland, S. R. Lewis, P. L. Read, J. В. Madeleine, 647 and F. Forget. The solsticial pause on Mars: 2mod-648 elling and investigation of causes. Icarus, 264:465-477,2016.649 10902643. 10.1016/j.icarus.2015.08.038. ISSN doi: URL 650 http://dx.doi.org/10.1016/j.icarus.2015.08.038. 651
- J.-B. Madeleine, F. Forget, Spiga, E. T. Navarro, Α. Millour, 652 and A. Määttänen. F. Montmessin, Global climate modeling 653 of the Martian water cycle with improved microphysics and ra-654 diatively active water ice clouds. Journal of Geophysical Re-655 ISSN 21699097. search: Planets, 119(7):1479–1495, jul 2014. doi: 656 10.1002/2013JE004550. URL http://arxiv.org/pdf/1310.1010.pdf 657 http://doi.wiley.com/10.1002/2013JE004550. 658
- C. E. Newman and M. I. Richardson. The impact of surface dust source
  exhaustion on the martian dust cycle, dust storms and interannual variability, as simulated by the MarsWRF General Circulation Model. *Icarus*,
  257:47-87, 2015. ISSN 10902643. doi: 10.1016/j.icarus.2015.03.030. URL
  http://dx.doi.org/10.1016/j.icarus.2015.03.030.

664 C. E. Newman, S. R. Lewis, P. P. L. Read, and F. F. For-665 get. Modeling the Martian dust cycle, 1. Representations of 666 dust transport processes. *Journal of Geophysical Research*, 107 (E12):5123, 2002. ISSN 0148-0227. doi: 10.1029/2002JE001910.
 URL http://doi.wiley.com/10.1029/2002JE001910
 http://oro.open.ac.uk/4504/.

H. R. Pruppacher and J. D. Klett. *Microphysics of Clouds and Precipitation*.
Springer, 2010.

M. I. Richardson, A. D. Toigo, and C. E. Newman. PlanetWRF: A
general purpose, local to global numerical model for planetary atmospheric and climate dynamics. *Journal of Geophysical Research*, 112(E9):
1-29, sep 2007. ISSN 0148-0227. doi: 10.1029/2006JE002825. URL
http://www.agu.org/pubs/crossref/2007/2006JE002825.shtml.

- A. D. Toigo, C. Lee, C. E. Newman, and M. I. Richardson. The impact of resolution on the dynamics of the martian global atmosphere:
  Varying resolution studies with the MarsWRF GCM. *Icarus*, 221(1):
  276-288, sep 2012. ISSN 00191035. doi: 10.1016/j.icarus.2012.07.020. URL
  http://linkinghub.elsevier.com/retrieve/pii/S0019103512002965.
- U. Ulbrich and P. Speth. The global energy cycle of stationary and transient atmospheric waves: Results from ECMWF analyses. *Meteorology and Atmospheric Physics*, 45(3-4):125–138, 1991. ISSN 01777971. doi: 10.1007/BF01029650.
- G. K. Vallis. Atmospheric and Oceanic Fluid Dynamics. Cambridge University Press, 2006.
- H. Wang. Dust storms originating in the northern hemisphere during the
   third mapping year of mars global surveyor. *Icarus*, 189(2):325–343, 2007.

- H. Wang and A. D. Toigo. The variability, structure and energy conversion
  of the northern hemisphere traveling waves simulated in a mars general
  circulation model. *Icarus*, 271:207–221, 2016.
- H. Wang, M. I. Richardson, R. J. Wilson, A. P. Ingersoll, A. D. Toigo, and
  R. W. Zurek. Cyclones, tides, and the origin of a cross-equatorial dust
  storm on mars. *Geophysical Research Letters*, 30(9), 2003.
- H. Wang, R. W. Zurek, and M. I. Richardson. Relationship between frontal
  dust storms and transient eddy activity in the northern hemisphere of mars
  as observed by mars global surveyor. *Journal of Geophysical Research: Planets*, 110(E7), 2005.
- H. Wang, M. I. Richardson, A. D. Toigo, and C. E. Newman. Zonal 700 wavenumber three traveling waves in the northern hemisphere of Mars 701 simulated with a general circulation model. Icarus, 223(2):654-676, 702 2013. ISSN 00191035. 10.1016/j.icarus.2013.01.004. doi: URL 703 http://dx.doi.org/10.1016/j.icarus.2013.01.004. 704
- R. J. Wilson, D. Banfield, B. J. Conrath, and M. D. Smith. Traveling
  waves in the Northern Hemisphere of Mars. *Geophysical Research Letters*,
  29(14):3-6, 2002. ISSN 0094-8276. doi: 10.1029/2002GL014866. URL
  http://www.agu.org/pubs/crossref/2002/2002GL014866.shtml.
- R. J. Wilson, G. A. Neumann, and M. D. Smith. Diurnal variation and
  radiative influence of martian water ice clouds. *Geophysical research letters*,
  34(2), 2007.

- M. J. Wolff and R. T. Clancy. Constraints on the size of Martian aerosols from
  Thermal Emission Spectrometer observations. *Journal of Geophysical Re- search*, 108(E9):5097, 2003. ISSN 0148-0227. doi: 10.1029/2003JE002057.
  URL http://doi.wiley.com/10.1029/2003JE002057.
- M. J. Wolff, M. D. Smith, R. T. Clancy, N. Spanovich, B. A. Whitney,
  M. T. Lemmon, J. L. Bandfield, D. Banfield, A. Ghosh, G. Landis, P. R.
  Christensen, J. F. Bell, and S. W. Squyres. Constraints on dust aerosols
  from the Mars Exploration Rovers using MGS overflights and Mini-TES. *Journal of Geophysical Research E: Planets*, 111(12):1–23, 2006. ISSN 01480227. doi: 10.1029/2006JE002786.